

MAP PROJECTION

The term *Projection* means the presentation of image on screen. A *Map Projection* means the representation of latitude and longitude of the globe on a flat sheet of paper. The network thus formed is called **graticule**.

As the earth's oblateness is little, the earth can be considered conveniently as a *Sphere*. The difficulty arises in the transfer of geographic grid from its actual spherical form (earth) to a flat surface (map). It is not possible to make a sheet of paper smoothly rounded like a sphere. Hence it appears impossible to prepare a correct map on a sheet of paper. Therefore we need to devise ways to present the earth's surface on a flat paper maintaining the area, shape, bearing, scale etc. as far as practicable by means of map projections.

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TABLE 2.1
Classification of Projections

Projections	Forms	Types
1. Zenithal Projections	(i) Perspective (ii) Non-Perspective	(i) Normal (Polar) (ii) Oblique (iii) Equatorial
2. Conical Projections	(i) Perspective (ii) Non-Perspective	(i) Normal
3. Cylindrical Projections	(i) Non-Perspective	(i) Equatorial (ii) Transverse (iii) Oblique
4. Conventional Projections		

The Gnomonic or Central Projection

$$\begin{aligned}
 \text{ii. } d &= \frac{\pi \times 5.77}{180} \times 10 \Rightarrow 1.097 \text{ cm} \\
 \text{iii. } r_o &= 5.77 \cot \phi \text{ cm (Table 2.13)} \\
 \text{iv. } d_o &= \frac{2\pi \times 5.77 \cos \phi}{360^\circ} \times 10^\circ \\
 &= 1.00705 \cos \phi \text{ cm (Table 2.14)}
 \end{aligned}$$

Cylindrical Equal-Area Projection

Principle

Lambert developed this projection in which a simple right circular cylinder touches the globe along the equator. Parallels and meridians are both projected as straight lines intersecting one another at right angles (Fig. 2.35). Tangential scale along all the parallels is kept equal to that along the equator. To maintain true area, radial scale along a meridian is made reciprocal to the tangential scale at that point. Hence, parallels lie at different heights above the equator. The interparallel spacing decreases rapidly towards the poles as parallels are all of same length as the equator.

In Fig. 2.33, let the cylinder ABCD touch the globe along the equator.

The parallel PQ is projected as straight line at PM distance away from WE.

$P_1Q_1 \parallel WE$ and $\angle POM = \phi$

Length of parallel (ϕ) on globe = $2\pi R \cos \phi$.

Length of parallel (ϕ) on projection = $2\pi R$.

$$\begin{aligned}
 \therefore \text{tangential scale} &= \frac{2\pi R}{2\pi R \cos \phi} \\
 &= \sec \phi \quad \dots (i)
 \end{aligned}$$

Let S be another parallel at $d\phi$ angle away from $P(\phi)$

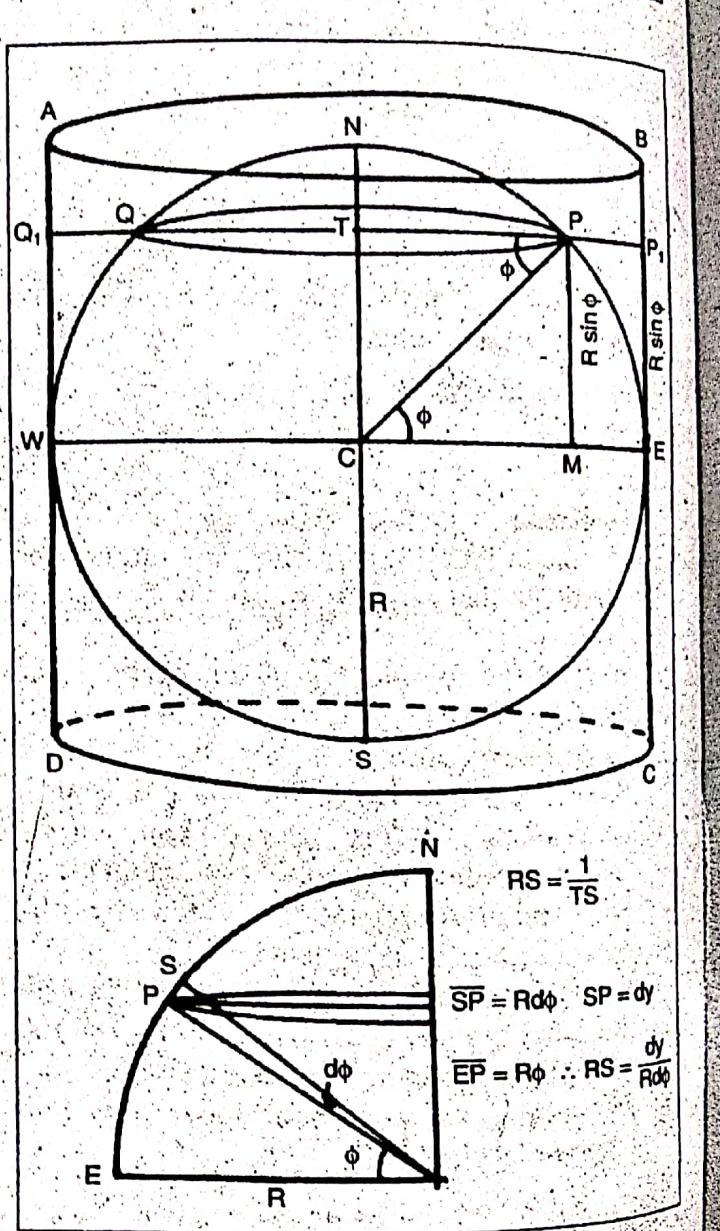


Fig. 2.35 Principles of Cylindrical Equal-Area Projection

\therefore the true angular distance of $d\phi$ on globe = $R \cdot d\phi$
 Let dy be the corresponding linear distance of $d\phi$ from the equator on projection.

$$\therefore \text{radial scale} = \frac{dy}{R.d\phi}$$

Since it is an equal area projection,
 radial scale \times tangential scale = 1

$$\text{or, } \frac{dy}{R.d\phi} \cdot \sec\phi = 1$$

$$\text{or, } dy = R \cos\phi \cdot d\phi$$

By integration,

$$\int dy = R \int \cos\phi \cdot d\phi$$

$$\therefore y = R \sin\phi$$

*

Theory

- Radius of the generating globe, R = Actual radius of the earth \div Denominator of R.F.
- Division along the equator for spacing the meridians at i° interval,

$$d = \frac{2\pi R}{360^\circ} \times i^\circ$$

- Height of any parallel above equator,
 $y_\phi = R \sin\phi$

Construction

- A straight line is drawn horizontally through the centre of the paper to represent the equator.
- It is then divided by d for spacing the meridians.

* Another Method:

From the diagram we get

$$\frac{PM}{OP} = \sin\phi \therefore PM = OP \sin\phi.$$

$$\therefore \text{Distance of parallel} = PM =$$

$$= y = R \sin\phi \quad [\text{where } OP = R]$$

- Through each of these division points, straight lines are drawn perpendicular to the equator to represent the meridians.
- On the central meridian, heights of different parallels (y_ϕ) from the equator are marked.
- Through each of these points, straight lines are drawn perpendicular to the central meridian to represent the parallels.
- The graticules are then properly labelled (Fig. 2.36).

Properties

- Parallels are represented by a set of parallel straight lines.
- Parallels are of same the length as the equator ($2\pi R$).
- Parallels are variably spaced on the meridians.
- Interparallel spacing decreases rapidly toward the pole.
- The tangential scale rapidly increases poleward and is infinity at the poles.
- Meridians are parallel straight lines truly spaced on the equator.
- Meridians are of same length equal to the diameter of the globe ($2R$).
- The intermeridian spacing is uniform on all the parallels.
- The pole is represented by a straight line of length $2\pi R$.

- x. At any point, the product of the two principal scales is unity.
- xi. It is an equal-area projection.
- xii. The shape is largely distorted near the poles.

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The intersections of the meridians with parallels are rectangular

Limitation : The scale along the equator is correct, but away from the equator the scale along the parallels becomes increasingly exaggerated; at the same time, the scale along the meridians becomes progressively diminished. The marked inequality between the scale along the parallels, and the scale along the meridians, leads to pronounced deformation of shape in high latitudes; in the polar regions for example, the projection is really of very little use.

Draw the graticules of Cylindrical Equal Area Projection extending between 50°N - 50°S and 20°W - 60°E at an interval of 10° . Scale 1: 60,000,000.

Calculation:

Step No. - 1 Radius of the Reduced earth

$$\begin{aligned} \left[\begin{array}{l} \text{Actual radius} \\ \text{of the earth} = \\ 640,000,000 \text{ cm} \end{array} \right] &= \frac{\text{Actual Radius of the earth}}{\text{Denominator of RF.}} \\ &= \frac{640,000,000 \text{ cm}}{60,000,000} \\ &= 10.6667 \text{ cm} \end{aligned}$$

Step No. - 2 Division along the equator for spacing the meridians

$$\begin{aligned} &= \frac{2\pi R}{360^{\circ}} \times \text{interval} \\ &= \frac{\pi}{180^{\circ}} \times \text{int.} \times R = \frac{\pi}{180^{\circ}} \times 10^{\circ} \times 10.6667 \\ &= 1.862 \text{ cm} \end{aligned}$$

Step No. - 3 Distance of parallels from the Equator = $y = R \sin \phi$

Latitude ϕ	R in cm	$\sin \phi$	$y = R \sin \phi$
0°	10.6667	0.0000	0.000 cm
10°	"	0.1736	1.852 "
20°	"	0.3420	3.648 "
30°	"	0.5000	5.333 "
40°	"	0.6428	6.856 "
50°	"	0.7660	8.171

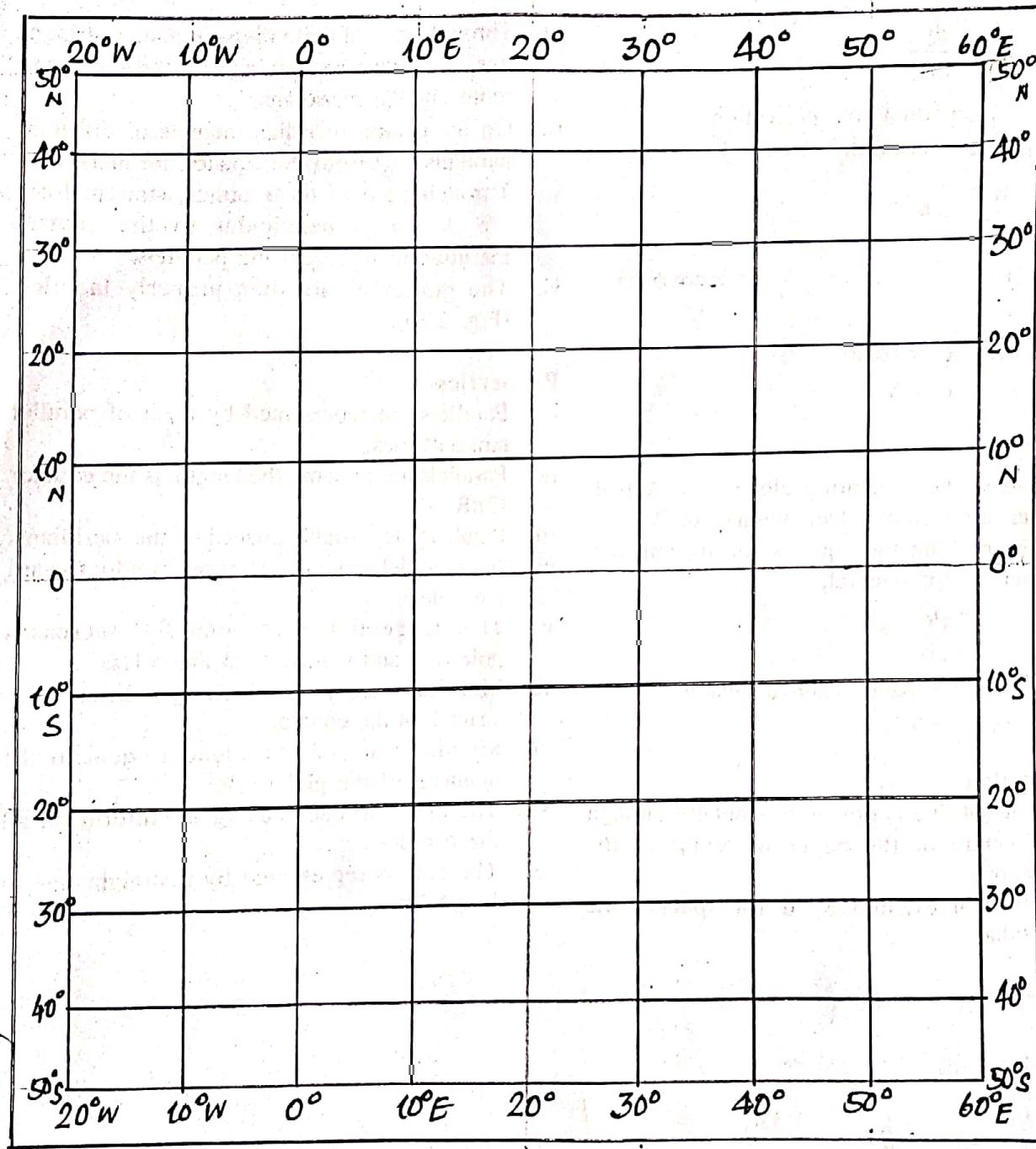


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Drawing Sheet

(A3 Size
Drawing Paper)
or Cartridge Paper)

CYLINDRICAL EQUAL-AREA
PROJECTION



Extension: $50^{\circ}N - 50^{\circ}S$
and $20^{\circ}W - 60^{\circ}E$

Scale 1 : 60,000,000